

# Markscheme

**May 2018**

**Physics**

**Higher level**

**Paper 3**

30 pages

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**Section A**

| Question |   | Answers  | Notes  | Total |
|----------|---|--|--|-------|
| 1.       | a | <p>distance fallen = <math>654 - 12 = 642</math> «mm» ✓</p> <p>absolute uncertainty = <math>2 + 0.1</math> «mm» <math>\approx 2 \times 10^{-3}</math> «m» <b>or</b> <math>2.1 \times 10^{-3}</math> «m» <b>or</b> <math>2.0 \times 10^{-3}</math> «m» ✓</p>  | Accept answers in mm or m  | 2     |
| 1.       | b | <p><math>\langle a = \frac{2s}{t^2} = \frac{2 \times 0.642}{0.363^2} \rangle = 9.744</math> «ms<sup>-2</sup>» ✓</p> <p>fractional uncertainty in distance = <math>\frac{2}{642}</math> <b>AND</b> fractional uncertainty in time = <math>\frac{0.002}{0.363}</math> ✓</p> <p>total fractional uncertainty = <math>\frac{\Delta s}{s} + 2 \frac{\Delta t}{t}</math> «= 0.00311 + 2 × 0.00551» ✓</p> <p>total absolute uncertainty = 0.1 <b>or</b> 0.14 <b>AND</b> same number of decimal places in value and uncertainty, ie: <math>9.7 \pm 0.1</math> <b>or</b> <math>9.74 \pm 0.14</math> ✓</p> | <p>Accept working in % for MP2 and MP3</p> <p>Final uncertainty must be the absolute uncertainty</p> | 4     |

| Question |   |   | Answers  | Notes   | Total |
|----------|---|---|--|---|-------|
| 2.       | a |   | <p>combines the two equations to obtain result</p> <p>«for example <math>\frac{1}{I} = K^2 (C + x)^2 = \frac{4\pi}{P} (C + x)^2</math>» ✓</p> <p><b>OR</b></p> <p>reverse engineered solution – substitute <math>K = 2\sqrt{\frac{\pi}{P}}</math> into <math>\frac{1}{I} = K^2 (C + x)^2</math> to get</p> <p><math>I = \frac{P}{4\pi(C + x)^2}</math> ✓</p> | <p><i>There are many ways to answer the question, look for a combination of two equations to obtain the third one</i></p> | 1     |
| 2.       | b | i | <p>extrapolating line to cross <math>x</math>-axis / use of <math>x</math>-intercept</p> <p><b>OR</b></p> <p>Use <math>C = \frac{y\text{-intercept}}{\text{gradient}}</math></p> <p><b>OR</b></p> <p>use of gradient and one point, correctly substituted in one of the formulae ✓</p> <p>accept answers between 3.0 and 4.5 «cm» ✓</p>                      | <p><i>Award [1 max] for negative answers</i></p>  | 2     |

(continued...)

(Question 2 continued)

| Question |   |    | Answers   | Notes   | Total |
|----------|---|----|---|---|-------|
| 2.       | b | ii | <p><b>ALTERNATIVE 1</b></p> <p>Evidence of finding gradient using two points <u>on the line</u> at least 10 cm apart ✓</p> <p>Gradient found in range: 115–135 <b>or</b> 1.15–1.35 ✓</p><br><p>Using <math>P = \frac{4\pi}{K^2}</math> to get value between <math>6.9 \times 10^{-4}</math> and <math>9.5 \times 10^{-4}</math> «W» and POT correct ✓</p> <p>Correct unit, W <b>and</b> answer to 1, 2 or 3 significant figures ✓</p><br><p><b>ALTERNATIVE 2</b></p> <p>Finds <math>I\left(\frac{1}{y^2}\right)</math> from use of one point (<math>x</math> and <math>y</math>) on the line with <math>x &gt; 6\text{cm}</math> and <math>C</math> from (b)(i) to use in <math>I = \frac{P}{4\pi(C+x)^2}</math> or</p> $\frac{1}{\sqrt{I}} = Kx + KC \quad \checkmark$ <p>Correct re-arrangement to get <math>P</math> between <math>6.9 \times 10^{-4}</math> and <math>9.5 \times 10^{-4}</math> «W» and POT correct ✓</p> <p>Correct unit, W <b>and</b> answer to 1, 2 or 3 significant figures ✓</p> | <p><i>For 3rd marking point if no unit given, assume answer is in W</i></p><br><p><i>Award [3 max] for an answer between 6.9W and 9.5W (POT penalized in 3rd marking point)</i></p><br><p><i>Alternative 2 is worth [3 max]</i></p> | 4     |

(continued...)

(Question 2 continued)

| Question |   | Answers   | Notes | Total |
|----------|---|---|-------|-------|
| 2.       | c | this graph will be a curve / not be a straight line ✓<br><br>more difficult to determine value of $K$<br><b>OR</b><br>more difficult to determine value of $C$<br><b>OR</b><br>suitable mathematical argument ✓ | OWTTE | 2     |

**Section B**

**Option A — Relativity**

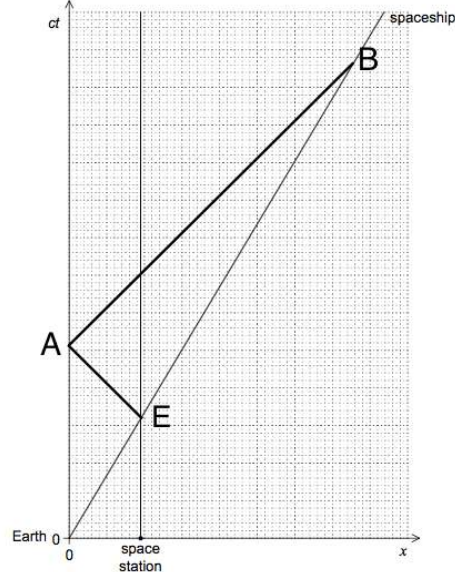
| Question |   |    | Answers  | Notes | Total |
|----------|---|----|--|-------|-------|
| 3.       | a | i  | 1.25c ✓  |       | 1     |
| 3.       | a | ii | <p><b>ALTERNATIVE 1</b></p> $u' = \frac{(0.50 + 0.75)}{1 + 0.5 \times 0.75} c \quad \checkmark$ <p>0.91c ✓</p> <p><b>ALTERNATIVE 2</b></p> $u' = \frac{-0.50 - 0.75}{1 - (-0.5 \times 0.75)} c \quad \checkmark$ <p>-0.91c ✓</p> |       | 2     |
| 3.       | b |    | nothing can travel faster than the speed of light (therefore (a)(ii) is the valid answer) ✓  | OWTTE | 1     |

| Question |   | Answers  | Notes | Total |
|----------|---|--|-------|-------|
| 4.       | a | <p>0.60c<br/> <b>OR</b><br/> <math>1.8 \times 10^8 \text{ «m s}^{-1}\text{»} \checkmark</math></p>   |       | 1     |
| 4.       | b | <p><b>ALTERNATIVE 1</b><br/>                     time interval in the Earth frame = <math>90 \times \gamma = 112.5</math> minutes <math>\checkmark</math><br/>                     «in Earth frame it takes 112.5 minutes for ship to reach station»<br/>                     so distance = <math>112.5 \times 60 \times 0.60c \checkmark</math><br/> <math>1.2 \times 10^{12} \text{ «m»} \checkmark</math></p> <p><b>ALTERNATIVE 2</b><br/>                     Distance travelled according in the spaceship frame = <math>90 \times 60 \times 0.6c \checkmark</math><br/>                     = <math>9.72 \times 10^{11} \text{ «m»} \checkmark</math><br/>                     Distance in the Earth frame «= <math>9.72 \times 10^{11} \times 1.25</math>» = <math>1.2 \times 10^{12} \text{ «m»} \checkmark</math></p> |       | 3     |

(continued...)



(Question 4 continued)

| Question |   |   | Answers   | Notes   | Total |
|----------|---|---|---|---|-------|
| 4.       | c |   | signal will take « $112.5 \times 0.60 \Rightarrow 67.5$ «minutes» to reach Earth «as it travels at $c$ »<br><b>OR</b><br>signal will take « $\frac{1.2 \times 10^{12}}{3 \times 10^8} \Rightarrow 4000$ «s» ✓<br>total time « $= 67.5 + 112.5$ » = 180 minutes <b>or</b> 3.00 h or 3:00am ✓ |   | 2     |
| 4.       | d | i | line from event E to A, upward and to left with A on $ct$ axis (approx correct) ✓<br>line from event A to B, upward and to right with B on $ct'$ axis (approx correct) ✓<br>both lines drawn with ruler at 45 (judge by eye) ✓  | eg:<br> | 3     |

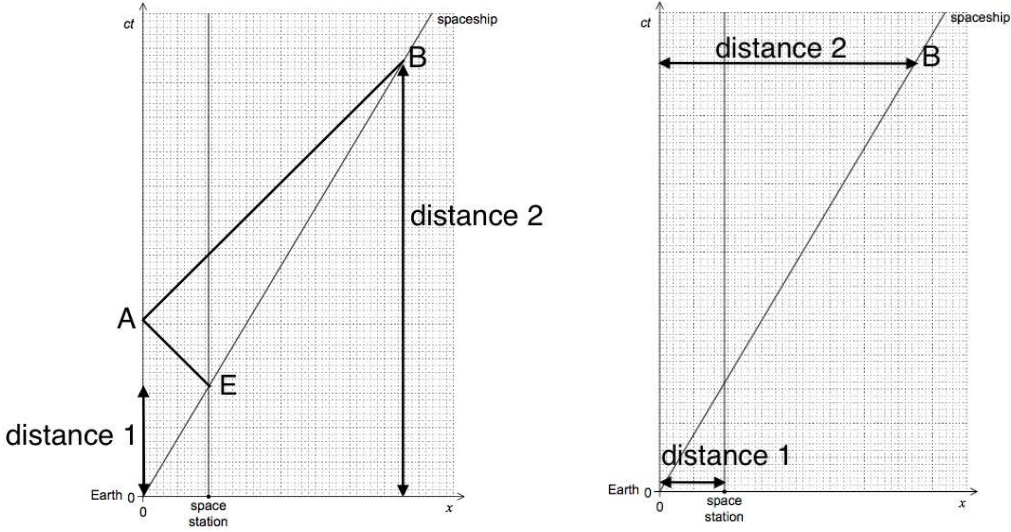
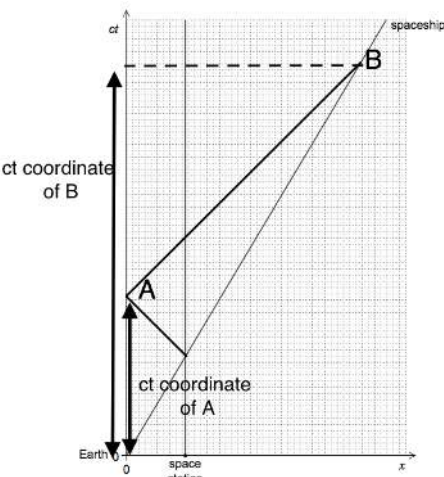
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(Question 4 continued)

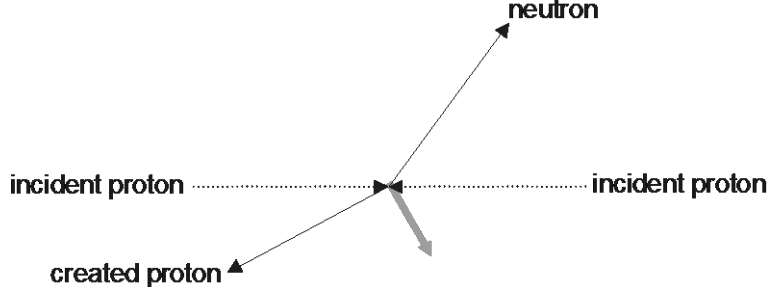
| Question |   |    | Answers  | Notes   | Total |
|----------|---|----|--|---|-------|
| 4.       | d | ii | <p><b>ALTERNATIVE 1</b></p> <p>«In spaceship frame»</p> <p>Finds the ratio <math>\frac{OB}{OE}</math> (or by similar triangles on <math>x</math> or <math>ct</math> axes), value is approximately 4 ✓</p> <p>hence time elapsed <math>\approx 4 \times 90\text{mins} \approx 6\text{h}</math> «so clock time is <math>\approx 6:00</math>» ✓</p> | <p><b>Alternative 1:</b></p> <p>Allow similar triangles using <math>x</math>-axis or <math>ct</math>-axis, such as <math>\frac{\text{distance 2}}{\text{distance 1}}</math> from diagrams below</p> | 2     |

(continued...)

(Question 4 continued)

| Question |   |    | Answers  | Notes   | Total |
|----------|---|----|--|---|-------|
| 4.       | d | ii | <p><b>ALTERNATIVE 2</b></p> <p>«In Earth frame»</p> <p>Finds the ratio <math>\frac{ct \text{ coordinate of B}}{ct \text{ coordinate of A}}</math>, value is approximately 2.5 ✓</p> <p>hence time elapsed <math>\approx \frac{2.5 \times 3h}{1.25} \approx 6h</math></p> <p>«so clock time is <math>\approx 6:00</math>» ✓</p> |  <p><b>ALTERNATIVE 2:</b></p>  |       |

| Question |   |    | Answers  | Notes | Total |
|----------|---|----|--|-------|-------|
| 5.       | a |    | quantity that is the same/constant in all inertial frames ✓  |       | 1     |
| 5.       | b | i  | spacetime interval = $27^2 - 15^2 = 504$ «m <sup>2</sup> » ✓   |       | 1     |
| 5.       | b | ii | <p><b>ALTERNATIVE 1</b></p> <p>Evidence of <math>x' = 0</math> ✓</p> $t' \text{ «} = \frac{\sqrt{504}}{c} \text{»} = 7.5 \times 10^{-8} \text{ «s»} \checkmark$ <p><b>ALTERNATIVE 2</b></p> $\gamma = 1.2 \checkmark$ $t' \text{ «} = \frac{9 \times 10^{-8}}{1.2} \text{»} = 7.5 \times 10^{-8} \text{ «s»} \checkmark$ |       | 2     |
| 5.       | c |    | <p>observer B measures the proper time and this is the shortest time measured</p> <p><b>OR</b></p> <p>time dilation occurs «for B's journey» according to A</p> <p><b>OR</b></p> <p>observer B is stationary relative to the particle, observer A is not ✓</p>   |       | 1     |

| Question |   |    | Answers   | Notes  | Total |
|----------|---|----|---|--|-------|
| 6.       | a |    | $\gamma \ll \frac{3350}{938} \gg = 3.57 \checkmark$   |  | 1     |
| 6.       | b | i  | energy of pion = $(3350 \times 2) - 6200 = 500 \ll \text{MeV} \gg \checkmark$<br>$500^2 = p^2 c^2 + 140^2 \checkmark$<br>$p = 480 \ll \text{MeV c}^{-1} \gg \checkmark$ |  | 3     |
| 6.       | b | ii | path of pion constructed in direction around 4–5 o'clock by eye $\checkmark$  | eg:<br> <p>The diagram shows a central collision point. A horizontal dotted line represents the path of an incident proton from the left. At the collision point, a solid arrow points up and to the right towards the label 'neutron'. Another solid arrow points down and to the left towards the label 'created proton'. A solid arrow points down and to the right from the collision point, representing the path of the pion. A second horizontal dotted line represents an incident proton from the right, which continues past the collision point.</p> | 1     |

| Question |   |    | Answers  | Notes | Total |
|----------|---|----|--|-------|-------|
| 7.       | a | i  | boundary inside which events cannot be communicated to an outside observer<br><b>OR</b><br>distance/surface at which escape velocity = $c$ ✓   | OWTTE | 1     |
| 7.       | a | ii | mass of black hole = $7.2 \times 10^{36}$ «kg» ✓<br><br>$\left\langle \frac{2GM}{c^2} \right\rangle = 1 \times 10^{10}$ «m» ✓  |       | 2     |
| 7.       | b |    | wherever S-2 is in orbit, time observed is longer than 5.0 s ✓<br>when closest to the star S-2 periodic time dilated more than when at greatest distance ✓<br>Justification using formula or time is more dilated in stronger gravitational fields ✓ |       | 2 max |

Option B — Engineering physics

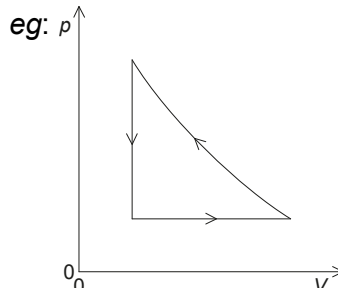
| Question |   |     | Answers  | Notes | Total |
|----------|---|-----|--|-------|-------|
| 8.       | a | i   | an object's resistance to change in rotational motion<br><b>OR</b><br>equivalent of mass in rotational equations ✓   | OWTTE | 1     |
| 8.       | a | ii  | $\Delta KE + \Delta \text{rotational KE} = \Delta GPE$<br><b>OR</b><br>$\frac{1}{2}mv^2 + \frac{1}{2}I\frac{v^2}{r^2} = mgh$ ✓<br><br>$\frac{1}{2} \times 0.250 \times v^2 + \frac{1}{2} \times 1.3 \times 10^{-4} \times \frac{v^2}{1.44 \times 10^{-4}} = 0.250 \times 9.81 \times 0.36$ ✓<br><br>$v = 1.2 \text{ « m s}^{-1} \text{ »}$ ✓ |       | 3     |
| 8.       | a | iii | $\omega \ll = \frac{1.2}{0.012} \gg = 100 \text{ « rad s}^{-1} \text{ »}$ ✓  |       | 1     |
| 8.       | b | i   | force in direction of motion ✓<br>so linear speed increases ✓  |       | 2     |
| 8.       | b | ii  | force gives rise to anticlockwise/opposing torque on wheel ✓<br>so angular speed decreases ✓   | OWTTE | 2     |

| Question |   | Answers   | Notes   | Total |
|----------|---|---|---|-------|
| 9.       | a | <p><b>ALTERNATIVE 1</b></p> <p>«Using <math>\frac{V_1}{T_1} = \frac{V_2}{T_2}</math> »</p> $V_2 = \frac{47.1 \times (273 + 19)}{(273 - 12)} \checkmark$ $V_2 = 52.7 \text{ «m}^3\text{»} \checkmark$ <p><b>ALTERNATIVE 2</b></p> <p>«Using <math>PV = nRT</math> »</p> $V = \frac{243 \times 8.31 \times (273 + 19)}{11.2 \times 10^3} \checkmark$ $V = 52.6 \text{ «m}^3\text{»} \checkmark$ |   | 2     |
| 9.       | b | $W \text{ «} = P\Delta V \text{»} = 11.2 \times 10^3 \times (52.7 - 47.1) \checkmark$ $W = 62.7 \times 10^3 \text{ «J»} \checkmark$   | <p>Accept <math>66.1 \times 10^3 \text{ J}</math> if 53 used</p> <p>Accept <math>61.6 \times 10^3 \text{ J}</math> if 52.6 used</p>   | 2     |
| 9.       | c | $\Delta U \text{ «} = \frac{3}{2} nR\Delta T \text{»} = 1.5 \times 243 \times 8.31 \times (19 - (-12)) = 9.39 \times 10^4 \checkmark$ $Q \text{ «} = \Delta U + W \text{»} = 9.39 \times 10^4 + 6.27 \times 10^4 \checkmark$ $Q = 1.57 \times 10^5 \text{ «J»} \checkmark$  | <p>Accept <math>1.60 \times 10^5</math> if <math>66.1 \times 10^3 \text{ J}</math> used</p> <p>Accept <math>1.55 \times 10^5</math> if <math>61.6 \times 10^3 \text{ J}</math> used</p> | 3     |

(continued...)



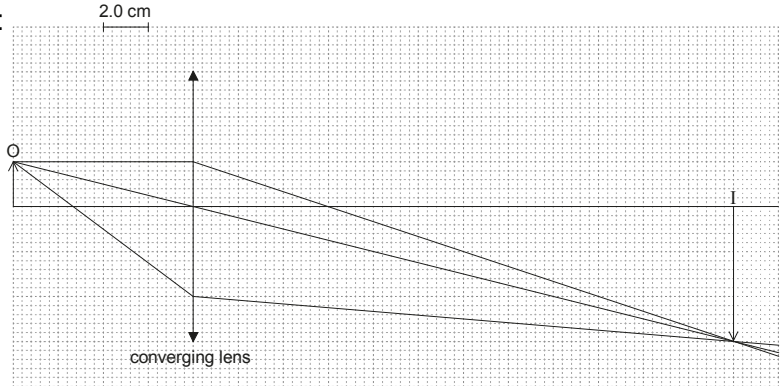
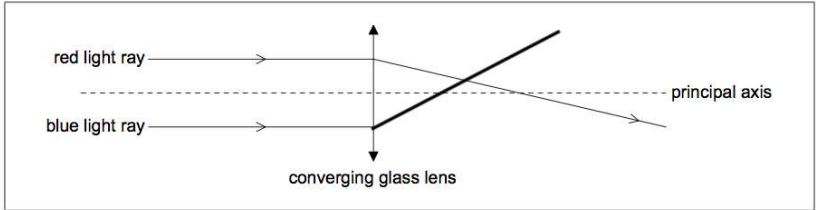
(Question 9 continued)

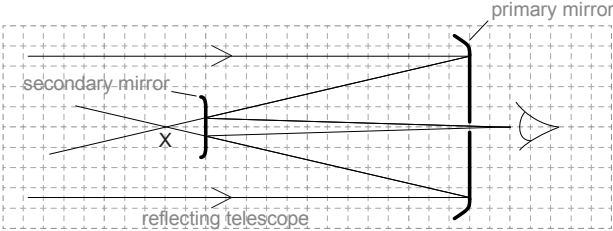
| Question |   |    | Answers  | Notes  | Total |
|----------|---|----|--|--|-------|
| 9.       | d | i  | concave curve from RHS of present line to point above LHS of present line ✓<br>vertical line from previous curve to the beginning ✓                          | eg: $p$<br> | 2     |
| 9.       | d | ii | energy is removed from the gas and so entropy decreases<br><b>OR</b><br>temperature decreases «at constant volume (less disorder)»<br>so entropy decreases ✓ | OWTTE  | 1     |
| 9.       | e |    | different paradigms/ways of thinking/modelling/views ✓<br>allows testing in different ways ✓<br>laws can be applied different situations ✓                   | OWTTE  | 1 max |

| Question |   | Answers  | Notes  | Total |   |
|----------|---|--|--|-------|---|
| 10.      | a | $\frac{1}{2} \rho v_x^2 = p_Y - p_X = \rho g \Delta h \quad \checkmark$ $v_x = \sqrt{2 \times 9.8 \times (0.32 - 0.10)} \quad \checkmark$ $v_x = 2.08 \text{ «ms}^{-1}\text{»} \quad \checkmark$ |  | 3     |   |
| 10.      | b | i  | $R = \left\langle \frac{vr\rho}{\eta} = \frac{2.1 \times 0.25 \times 10^3}{8.9 \times 10^{-4}} \right\rangle 5.9 \times 10^5 \quad \checkmark$ | 1     |   |
| 10.      | b | ii   | ( $R > 1000$ ) flow is not laminar, so assumption is invalid $\checkmark$  | OWTTE | 1 |

| Question |   | Answers  | Notes | Total |
|----------|---|--|-------|-------|
| 11.      | a | general shape as shown $\checkmark$<br>peak at 6 kHz $\checkmark$<br>graph does not touch the $f$ axis $\checkmark$  |       | 3     |
| 11.      | b | peak broadens $\checkmark$<br>reduced maximum amplitude / graph shifted down $\checkmark$<br>resonant frequency decreases / graph shifted to the left $\checkmark$ |       | 2 max |

Option C — Imaging

| Question |   |    | Answers  | Notes  | Total |
|----------|---|----|--|--|-------|
| 12.      | a | i  | <p>constructs ray parallel to principal axis and then to image position</p> <p><b>OR</b></p> <p><math>u = 8\text{cm}</math> and <math>v = 24\text{cm}</math> and lens formula ✓</p> <p>6 «cm» ✓</p>  | <p>eg:</p>  <p>converging lens</p> <p>Allow answers in the range of 5.6 to 6.4 cm</p>                   | 2     |
| 12.      | a | ii | <p><math>m = \text{«-»}3.0</math> ✓</p>  |  | 1     |
| 12.      | b |    | <p>completes diagram with blue focal point closer to lens ✓</p> <p>blue light/rays refracted/deviated more</p> <p><b>OR</b></p> <p>speed of blue light is less than speed of red light ✓</p> <p><b>OR</b></p> <p>different colors/wavelengths have different focal points/converge at different points ✓</p> | <p>First marking point can be explained in words or seen on diagram</p>  <p>converging glass lens</p> | 2     |

| Question |   | Answers  | Notes   | Total |
|----------|---|--|---|-------|
| 13.      | a | where the extensions of the reflected rays from the primary mirror would meet, with construction lines ✓   | eg:  | 1     |
| 13.      | b | greater magnification ✓  |   | 1     |
| 13.      | c | «use of $\frac{1.22\lambda}{d}$ to get» resolution of $6.7 \times 10^{-9}$ «rad» ✓<br><br>$\frac{5.8 \times 10^{-7}}{6.7 \times 10^{-9}} = 87$ «m» ✓<br><br>some reference to difficulty in making optical mirrors/lenses of this size ✓ | Allow $\frac{5.8 \times 10^{-7}}{5.5 \times 10^{-9}} = 105$ «m»                         | 3     |

| Question |   |     | Answers   | Notes  | Total |
|----------|---|-----|---|--|-------|
| 14.      | a |     | $\text{sinc} = \frac{1.4444}{1.4475}$ <i>or</i> $\text{sinc} = 0.9978$ ✓<br>critical angle = $86.2^\circ$ » ✓<br>with cladding only rays travelling nearly parallel to fibre axis are transmitted<br><b>OR</b><br>pulse broadening/dispersion will be reduced ✓ | OWTTE  | 3     |
| 14.      | b | i   | $\text{attenuation} = \ll 10 \log \frac{I}{I_0} \gg = 10 \log \frac{2.0 \times 10^{-6}}{400 \times 10^{-6}}$ ✓<br>$\text{attenuation} = \ll - \gg 23$ «dB» ✓  | Accept $10 \log \frac{400}{2.0}$ for first marking point | 2     |
| 14.      | b | ii  | $185 \times 0.200 = 37$ loss over length of cable ✓<br>$\ll \frac{37 - 23}{12} = 1.17 \gg$ so two amplifiers are sufficient ✓   |  | 2     |
| 14.      | b | iii | mention of material dispersion ✓<br>mention that rays become separated in time<br><b>OR</b><br>mention that ray A travels slower/arrives later than ray B ✓   |  | 2     |

(continued...)

(Question 14 continued)

| Question |   | Answers  | Notes  | Total        |
|----------|---|--|--|--------------|
| 14.      | c | high bandwidth/data transfer rates ✓<br>low distortion/Low noise/Faithful reproduction ✓<br>high security ✓<br>fast «fibre» broadband/internet ✓<br>high quality optical audio ✓<br>medical endoscopy ✓  | <i>Allow any other verifiable sensible advantage</i> | <b>1 max</b> |
| 15.      | a | many/array of transducers send ultrasound through body/object ✓<br>B scan made from many A scans in different directions ✓<br>the reflection from organ boundaries gives rise to position ✓<br>the amplitude/size gives brightness to the B scan ✓<br>2D/3D image formed «by computer» ✓ |  | <b>3 max</b> |

(continued...)

(Question 15 continued)

| Question |   |     | Answers   | Notes   | Total |
|----------|---|-----|---|---|-------|
| 15.      | b | i   | the thickness of tissue that reduces the intensity «of the X-rays» by a half<br><b>OR</b><br>$x_{\frac{1}{2}} = \frac{\ln 2}{\mu}$ where $x_{\frac{1}{2}}$ is the half value thickness and $\mu$ is attenuation coefficient ✓   | <i>Symbols must be defined for mark to be awarded</i> | 1     |
| 15.      | b | ii  | after fat layer, $I_{\text{fat}} = I_0 e^{-0.4499 \times 5.00}$ ✓<br>after muscle layer, $I = I_{\text{fat}} e^{-0.8490 \times 4.00}$ ✓<br>$I = 0.003533 I_0$ <b>or</b> 0.35% ✓   |   | 3     |
| 15.      | b | iii | «high energies factors:»<br>less attenuation/more penetration ✓<br>more damage to the body ✓<br>«so» stronger signal leaves the body<br><b>OR</b><br>«so» used in «most» medical imaging techniques ✓<br>«low energy factors:»<br>must be used with enhancement techniques ✓<br>greater attenuation/less penetration ✓<br>«so» more damage to the body «on surface layers»<br><b>OR</b><br>«so» unwanted in «most» medical imaging techniques ✓ |   | 3 max |

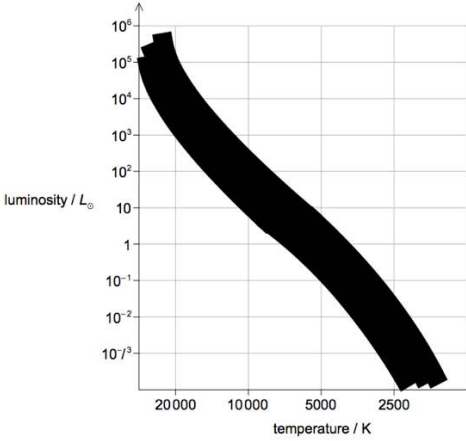
Option D — Astrophysics

| Question |   |    | Answers  | Notes | Total |
|----------|---|----|--|-------|-------|
| 16.      | a |    | photon/fusion/radiation force/pressure balances gravitational force/pressure ✓<br>gives both directions correctly (outwards radiation, inwards gravity) ✓  | OWTTE | 2     |
| 16.      | b |    | « $L \propto M^{3.5}$ for main sequence »<br>luminosity of $P = 2.5$ «luminosity of the Sun» ✓   |       | 1     |
| 16.      | c | i  | $L_{Gacrux} = 5.67 \times 10^{-8} \times 4\pi \times (58.5 \times 10^9)^2 \times 3600^4$ ✓<br>$L_{Gacrux} = 4.1 \times 10^{29}$ «W» ✓<br>$\frac{L_{Gacrux}}{L_{\odot}} \ll = \frac{4.1 \times 10^{29}}{3.85 \times 10^{26}} \gg = 1.1 \times 10^3$ ✓ |       | 3     |
| 16.      | c | ii | if the star is too far then the parallax angle is too small to be measured<br><b>OR</b><br>stellar parallax is limited to closer stars ✓   | OWTTE | 1     |

(continued...)



(Question 16 continued)

| Question |   |    | Answers   | Notes   | Total |
|----------|---|----|---|---|-------|
| 16.      | d | i  | line or area roughly inside shape shown – judge by eye ✓              | <p>Accept straight line or straight area at roughly 45°</p>  | 1     |
| 16.      | d | ii | P between $1 L_{\odot}$ and $10^1 L_{\odot}$ on main sequence drawn ✓ |   | 1     |

(continued...)

(Question 16 continued)

| Question |   |     | Answers   | Notes | Total |
|----------|---|-----|---|-------|-------|
| 16.      | d | iii | at $10^3 L_{\odot}$ , further to right than 5000 K and to the left of 2500 K (see shaded region)✓ |       | 1     |

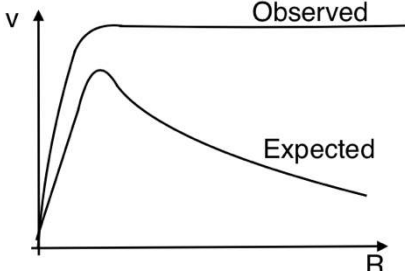
(continued...)

(Question 16 continued)

| Question |   | Answers   | Notes                       | Total |
|----------|---|---|-----------------------------|-------|
| 16.      | e | <p><b>ALTERNATIVE 1</b></p> <p>Main sequence to red giant ✓</p> <p><u>planetary nebula</u> with <u>mass</u> reduction/loss</p> <p><b>OR</b></p> <p><u>planetary nebula</u> with mention of remnant <u>mass</u> ✓</p> <p>white dwarf ✓</p> <p><b>ALTERNATIVE 2</b></p> <p>Main sequence to red supergiant region ✓</p> <p><u>Supernova</u> with <u>mass</u> reduction/loss</p> <p><b>OR</b></p> <p><u>Supernova</u> with mention of remnant <u>mass</u> ✓</p> <p>neutron star</p> <p><b>OR</b></p> <p>Black hole ✓</p> | OWTTE for both alternatives | 3     |

| Question |   | Answers  | Notes   | Total |
|----------|---|--|---|-------|
| 17.      | a | <p>use of gradient or any coordinate pair to find <math>H_0 \llcorner = \frac{v}{d} \llcorner</math> or <math>\frac{1}{H_0} \llcorner = \frac{d}{v} \llcorner \checkmark</math></p> <p>convert Mpc to m and km to m «for example <math>\frac{82 \times 10^3}{10^6 \times 3.26 \times 9.46 \times 10^{15}} \llcorner \checkmark</math></p> <p>age of universe <math>\llcorner = \frac{1}{H_0} \llcorner = 3.8 \times 10^{17} \llcorner \llcorner \text{«s»} \llcorner \checkmark</math></p> | <p>Allow final answers between <math>3.7 \times 10^{17}</math> and <math>3.9 \times 10^{17} \llcorner \llcorner \text{«s»} \llcorner</math> or <math>4 \times 10^{17} \llcorner \llcorner \text{«s»} \llcorner</math></p> | 3     |
| 17.      | b | <p>non-accelerated/uniform rate of expansion</p> <p><b>OR</b></p> <p><math>H_0</math> constant over time <math>\checkmark</math></p>   | OWTTE   | 1     |
| 17.      | c | <p><math>z \llcorner = \frac{v}{c} \llcorner = \frac{4.6 \times 10^4 \times 10^3}{3.00 \times 10^8} = 0.15 \llcorner \checkmark</math></p> <p><math>\frac{R}{R_0} = \llcorner z + 1 \llcorner = 1.15 \llcorner \checkmark</math></p> <p><math>\frac{R_0}{R} = \llcorner \frac{1}{1.15} \llcorner = 0.87</math></p> <p><b>OR</b></p> <p>87 % of the present size <math>\checkmark</math></p>  |   | 3     |

| Question |   | Answers   | Notes                  | Total |
|----------|---|---|------------------------|-------|
| 18.      | a | <p>«For a star to form»: magnitude of PE of gas cloud &gt; KE of gas cloud<br/> <b>OR</b><br/>                     Mass of cloud &gt; Jean's mass<br/> <b>OR</b><br/>                     Jean's criterion is the critical mass ✓<br/>                     hence a hot diffuse cloud could have KE which is too large/PE too small<br/> <b>OR</b><br/>                     hence a cold dense cloud will have low KE/high PE<br/> <b>OR</b><br/>                     a cold dense cloud is more likely to exceed Jeans mass<br/> <b>OR</b><br/>                     a hot diffuse cloud is less likely to exceed the Jeans mass ✓</p> | Accept $E_p + E_k < 0$ | 2     |
| 18.      | b | <p>Neutron capture creates heavier isotopes / heavier nuclei / more unstable nucleus ✓<br/> <u><math>\beta^-</math> decay</u> of heavy elements/iron increases atomic number «by 1» ✓</p>   | OWTTE                  | 2     |

| Question |   | Answers   | Notes  | Total |
|----------|---|---|--|-------|
| 19.      | a | <p>«rotational» velocity of stars are expected to decrease as distance from centre of galaxy increases ✓</p> <p>the observed velocity of outer stars is constant/greater than predicted ✓</p> <p>implying large mass on the edge «which is dark matter» ✓</p>   | <p>OWTTE</p> <p>1st and 2nd marking points can be awarded from an annotated sketch with similar shape as the one below</p>  | 3     |
| 19.      | b | <p>data from <u>type 1a supernovae</u> shows universe expanding at an accelerated rate ✓</p> <p>gravity was expected to slow down the expansion of the universe</p> <p><b>OR</b></p> <p>this did not fit the hypotheses at that time ✓</p> <p>dark energy counteracts/opposes gravity</p> <p><b>OR</b></p> <p>dark energy causes the acceleration ✓</p> | OWTTE  | 3     |